CIS 761. Database Management Systems Lecture notes on "The Chase"

Torben Amtoft

March 12, 2005

A typical problem

Assume that the relation r satisfies the functional dependency

$$A \rightarrow B$$

and the multi-valued dependency

$$B \rightarrow \rightarrow C$$
.

We want to use the above dependencies to simplify the query q given by

$$q = \Pi_{ABD}(r) \bowtie \Pi_{AC}(r).$$

The solution

Assume that t is a tuple in q. Let t=(a,b,c,d), then we know that $(a,b,d) \in \Pi_{ABD}(r)$ and that $(a,c) \in \Pi_{AC}(r)$. Therefore, there exists c',b',d' such that r contains the tuples

$$\begin{array}{c|cccc}
A & B & C & D \\
\hline
a & b & c' & d \\
a & b' & c & d'
\end{array}$$

Since r satisfies $A \to B$, we infer that b = b', and the situation is therefore that r contains the tuples

$$\begin{array}{c|cccc}
A & B & C & D \\
\hline
a & b & c' & d \\
a & b & c & d'
\end{array}$$

and since r satisfies $B \to \to C$, r also contains the tuples

In particular, we see that $t=(a,b,c,d)\in r$. Since t was an arbitrary tuple in q, this shows that $q\subseteq r$. Clearly, $r\subseteq q$, so q=r. Thus, the complex query q can be reduced to the simple query r.

For more material on "the chase", see [Abiteboul & Hull & Vianu, 1995].