Exercise Sheet 12 CS 2210 Logic for Computer Scientists (Hitzler) Solutions due: Tuesday April 16, 2015, 11am

Exercise 61 Show, that, for any formula F in which y does not occur as free variable, $\forall xF \equiv \forall yF[x/y]$.

Exercise 62 Transform all formulas from Example 3.1.5 into NNF.

Exercise 63 Show, using a tableau, that $\exists x(P(x) \land Q(x)) \models \exists x P(x) \land \exists y Q(y)$.

Exercise 64 Show, using a tableau, that $\exists x(O(s,x) \land A(x))$ is a logical consequence of the formulas in Example 3.1.5.

Exercise 65 Show, using a tableau, that $Q(a) \wedge Q(b) \wedge \forall x (P(x) \wedge (Q(x) \rightarrow \neg P(x)))$ is unsatisfiable.