

**Exercise Sheet 6**  
**CS 2210 Logic for Computer Scientists (Hitzler)**  
**Solutions due: Tuesday October 14, 2014, 9:30am**

**Exercise 33** Express modus tollens, modus tollendo ponens, and modus ponendo tollens in propositional logic.

**Exercise 34** Show, using truth tables, that the modi from Exercise 33 are valid.

**Exercise 35** For  $P$  the Datalog program from Exercise 9, determine  $v(P)$ .

**Exercise 36** Translate the “secrets” of the centenarian (slide 13 of the slideset from the first session) into formulas, where  $B$  stands for *beer for dinner*,  $F$  for *fish for dinner* and  $I$  for *ice cream for dinner*.

**Exercise 37** Show that the claim on slide 13 holds.

**Exercise 38** Transform  $\neg((A \vee B) \wedge (C \vee D) \wedge (E \vee F))$  into CNF.

**Exercise 39** Give a CNF for the formula  $F$  in Remark 2.5.7.

**Exercise 40 (no hand-in)** Show by structural induction: For any formula  $F$  (with all brackets written), we have  $b(F) \leq c(F)$ , where  $b(F)$  is the number of all opening brackets in  $F$ , and  $c(F)$  is the number of all connectives in  $F$ .

**Exercise 41 (no hand-in)** Show the following: For all formulas  $F_i$  ( $i = 1, 2, 3$ ),  $F_1 \vee (F_2 \wedge F_3)$  and  $(F_1 \vee E) \wedge (E \leftrightarrow (F_2 \wedge F_3))$  are equisatisfiable ( $E$  is a propositional variable not occurring in  $F_1, F_2, F_3$ ).