

Neural-Symbolic Integration

Bridging the gap between subsymbolic neural networks and symbolic logic

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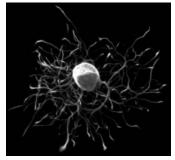
Contents



- 1. Why neural-symbolic integration?
- 2. Earlier work
- 3. The neural-symbolic learning cycle
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- 5. The cycle for first-order logic
 - a. The Core Method
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Neural-symbolic Integration





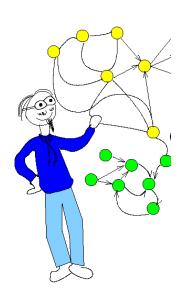


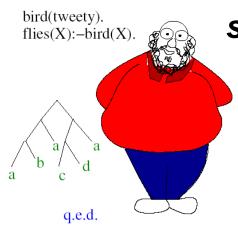
Why neural-symbolic integration?



connectionism

Neural-symbolic Integration





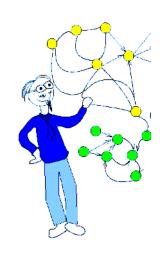
symbolic Al

- Artificial neural networks and symbolic Al are two fundamentally different paradigms in Al.
- Their strengths and weaknesses are complementary.
- Neural-symbolic Integration is about integrating the paradigms while retaining their strengths.



Artificial neural networks





- Powerful machine-learning paradigm.
- Inspired by Biology/Neuroscience.
- Learning from noisy data possible.
- Robust. Graceful degradation.



- Recursive structures difficult.
- Cannot learn with background knowledge.





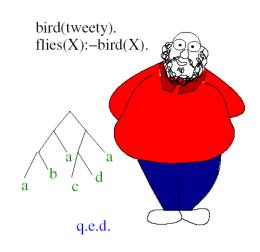
Knowledge representation/symbolic Al € kno.∈.sis

- Logic-based. Declarative.
- Modelled from human thinking.
- Explicit coding of knowledge.
- Highly recursive.

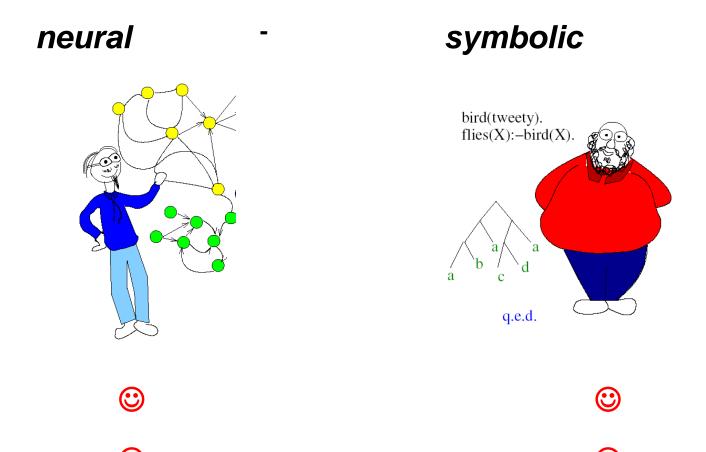


- Learning is difficult.
- Hardly tolerant against noise.
- Reasoning has high computational complexity.





Knowledge representation/symbolic Alekno.e.sis



realising connectionist processing of symbolic knowledge



The four main problems of NeSy



- Connectionist representation of symbolic knowledge.
- Extraction of symbolic knowledge from artificial neural networks.
- Connectionist learning of symbolic knowledge.
- Learning under background knowledge.

Besides ...



... the technical motivation just given:

- neural-symbolic integration is about the study from a computer science perspective – how knowledge can be processed within models of the brain
- standard artificial neural networks appear to be insufficient to capture human knowledge processing
- logic also appears to be insufficient to capture human knowledge processing

Driving motivation

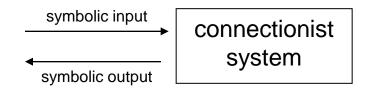


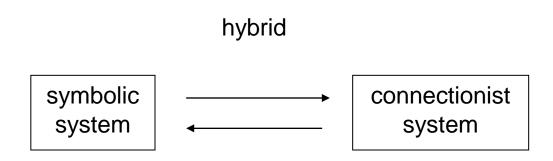
- Our approach is mainly computer-science-driven.
 - realisation of intelligent systems
- It contributes only indirectly to the question, how humans model reality and think about it.
- At hindsight, our approach probably rather shows, how humans do not model reality and think about it.
- Generally, neural-symbolic research requires more input from recent developments in neuroscience!

Hybrid vs. Integrated Approach



integrated





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Earlier work



- McCulloch & Pitts 1943
 - Neurons with binary activation functions.
 - Modelling of propositional connectives.
 - Networks equivalent to finite automata.

Values 0 ("false") and 1 ("true") being propagated.

$$\begin{array}{c}
1 \\
\hline
1
\end{array}$$
0.5
$$\begin{array}{c}
1 \\
\end{array}$$
disjunction

Simultaneous update of all nodes in network.

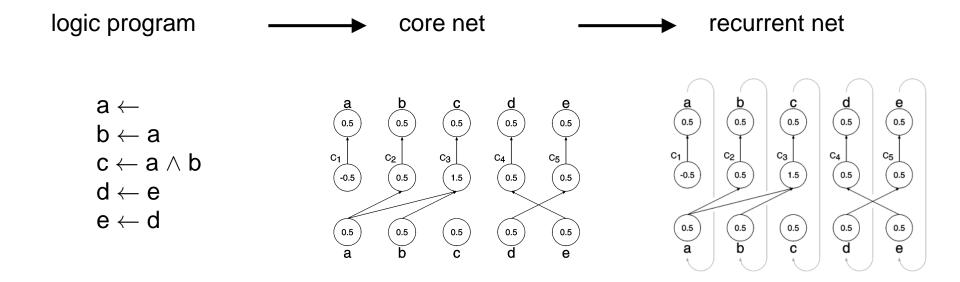
$$\begin{array}{c}
1 \\
1.5
\end{array}$$
1 conjunction

$$-1$$
 (-0.5) 1 negation

The propositional Core Method

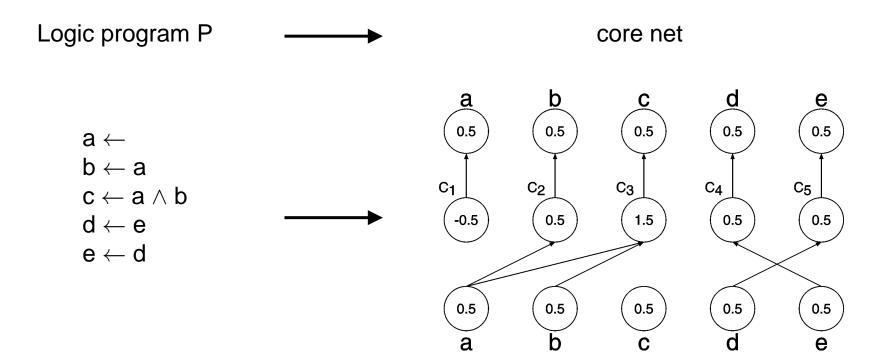


- Hölldobler & Kalinke 1994
 - Extends the approach by McCulloch & Pitts.
 - Representation of propositional logic programs and their semantics.
 - "Massively parallel reasoning."



The propositional Core Method



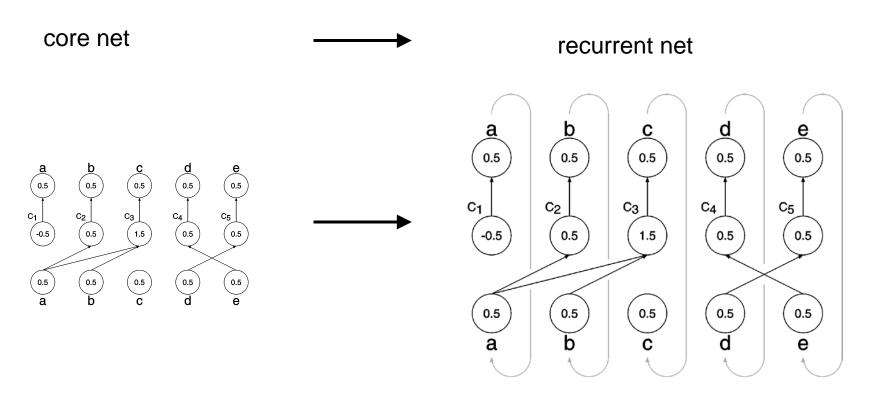


- Update "along implication".
- Corresponds to computing the semantic operator T_P.
- T_P represents meaning (semantics) of P through its fixed points.



The propositional Core Method



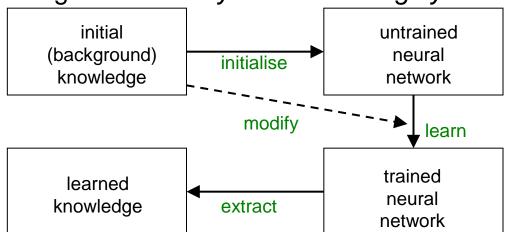


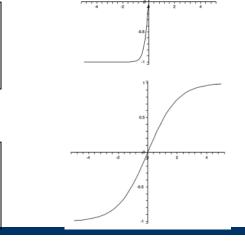
- Repeated updates along layers corresponds to iterations of the semantic operator.
- Semantics of the program (= fixed point of the operator) can be computed in a parallel manner.



CILP - Connectionist Inductive Logic Prog: Kno. E. SIS

- Garcez & Zaverucha 1999
 Garcez, Broda & Gabbay 2001
- Development of a learning paradigm from the Core Method.
- Required: differentiable activation function.
 - Allows learning with standard methods.
 - Backpropagation algorithm.
- Establishing the neural-symbolic learning cycle.

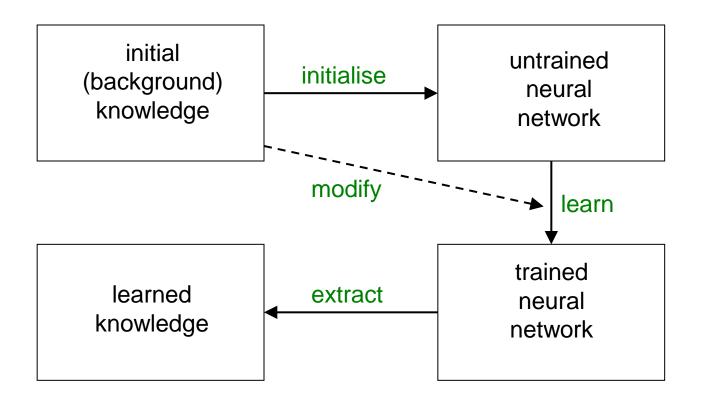






The neural-symbolic learning cycle





The four main problems of Neural-symbolic Integration.

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Conectionism and first-order predicate logic kno. s.s.s

 Connectionist representation of PL-knowledge very hard to realise.

McCarthy 1988: "Propositional fixation."

We need to capture the infinite in a finite way.

- infinite ground instantiations
 (∀x) male(x) ∧ hasSon(x,son(x)) → father(x)
- term representations member(X, [a,b,c | [d,e]])
- variable bindingsmale(x) ∧ hasSon(x,y) → father(x)



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PL Core Method



Hölldobler, Kalinke, Störr 1999
 Hitzler, Hölldobler, Seda 2004

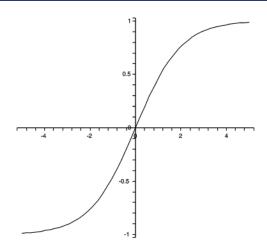
Idea:

- Use results by Funahashi 1989: "Every continuous function on the reals is approximable by standard feedforward networks."
- Hence: Consider logic programs for which T_P-operator is continuous in this sense.

Funahashi 1989 (simplified)



- σ sigmoidal activation function
- $K \subseteq \mathcal{R}_{compact}$
- f: $K \to \mathcal{R}$ continuous
- ε > 0

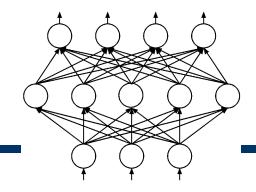


Then there exists a three-layer feedforward network with activation function σ and I/O-function F, so that

$$\max_{x \in \mathsf{K}} \{d(\mathsf{f}(x), \mathsf{F}(x))\} < \varepsilon.$$

Here d is a metric which induces the natural topology on \mathcal{R} .

I.e. continuous functions can be *uniformly* approximated by such networks with arbitrary accuracy.



Continuity of T_P – I



Hitzler, Hölldobler, Seda 2004

Let \mathcal{B}_A be the set of all body atoms in ground instantiated clauses of P with head A.

 $T_P: I_P \rightarrow I_P$ is called *locally finite*, if for all atoms A and all $I \in I_P$ there exists a finite $S \subseteq \mathcal{B}_A$, such that $T_P(J)(A) = T_P(I)(A)$ for all $J \in I_P$ which coincide with I on S.

$$p(s(x)) \leftarrow p(x).$$
 $p(0)$
 $p(x) \leftarrow p(s(x)).$
e.g. $\mathcal{B}_{p(s(0))} = \{p(0), p(s(s(0)))\}$

Continuity of T_P – II



$$T_P: I_P \rightarrow I_P$$
 is locally finite iff

T_P is continuous in Cantor space.

- Cantor-continuity is continuity wrt. the Cantor topology on the Cantor set.
- The Cantor topology is homeomorphic to the prefix-distance on (infinite) binary trees.
- The Cantor topology is homeomorphic to the subspace topology which is induced on a subset of \mathcal{K} which is compact, totally disconnected and dense in itself.



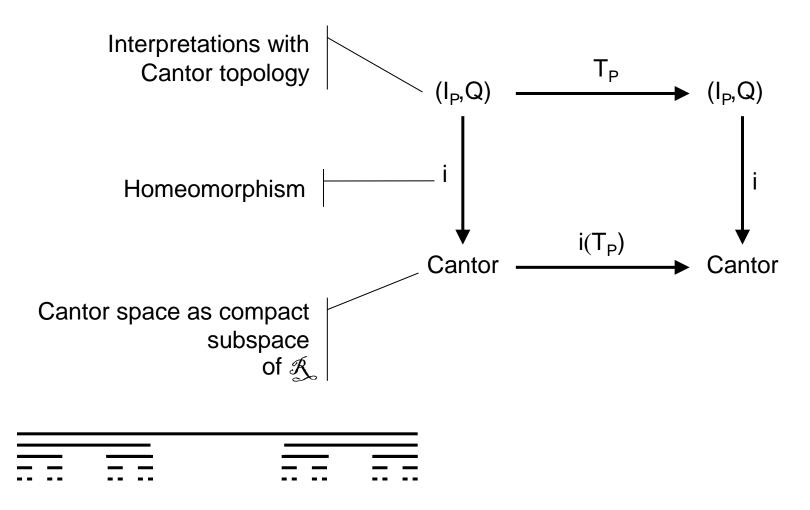
Continuity of T_P – III



- There are (uncontably) many homeomorphisms which map I_P with the Cantor topology into suitable subsets of A_E
- Locally finiteness is a logical (topology-free)
 characterisation of logic programs which can be
 represented in a a connectionist way in the sense of
 Funahashi.
- Problem: this argumentation is not constructive!

Relationship of I_P to Cantor Space





The Cantor topology as a paradigm bridgeno. e.s.s

- Connectionist side:
 - Cantor topology is a subtopology of the usual topology on the real numbers
- Logic Programming side:
 - Cantor topology captures useful notions of convergence of semantic operators, e.g.
 If T_Pⁿ → I (for n→∞), then I is a model of P.

Contents

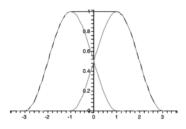


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Realising the cycle: Representation of logice kno. e. s is

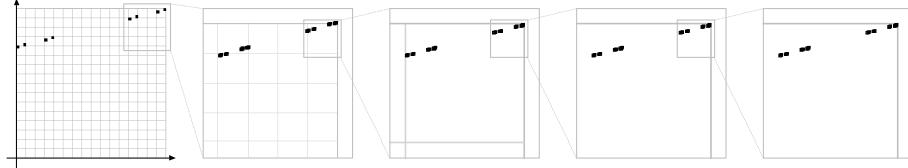
- Bader, Hitzler, Hölldobler, Witzel IJCAI-07
 - Algorithm for the approximate construction of neural networks from logic programs.
 - Realised for
 - RBS nets with triangular activation function
 - RBF nets with raised cosine activation function

$$\tau_{w,h,m}(x) = \begin{cases} \frac{h}{2} \cdot \left(1 + \cos\left(\frac{\pi(x-m)}{w}\right)\right) & \text{if } |x-m| < w \\ 0 & \text{otherwise} \end{cases}$$

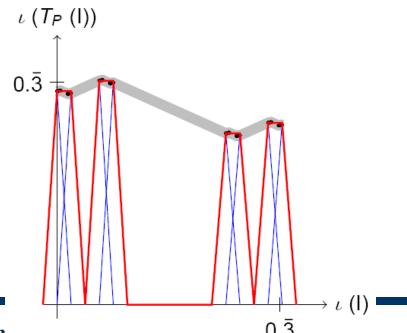


Realising the cycle (representation)



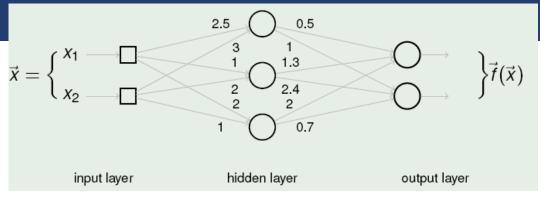


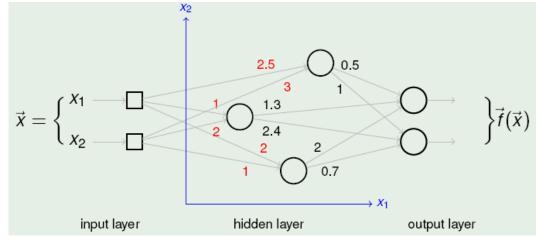
- Graph of T_P is a fractal.
- Approximation up to arbitrary precision possible.
- Requires quite some calculation to get correct parameters in higher dimensions ...

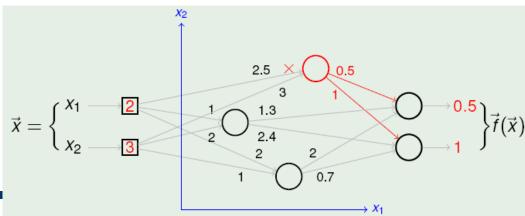














WSU

input layer

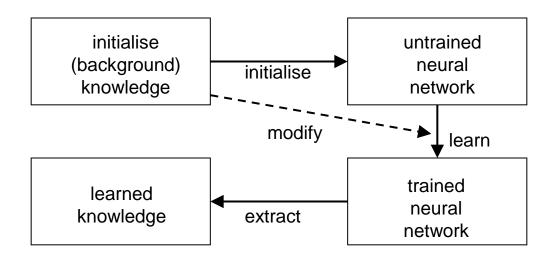
hidden layer

output layer

Realising the cycle: learning



- Reuse of standard network architecture allows to use known and powerful learning methods.
 - Backpropagation
 - We merged in techniques from Supervised Growing Neural Gas (SGNG) [Fritzke 1998].



Realising the cycle: Implementation

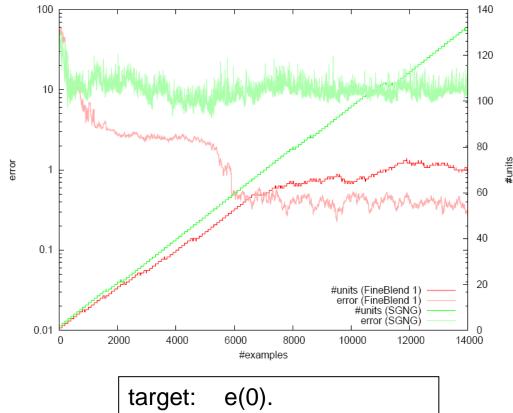


- Bader & Witzel, first prototype
- JDK 1.5 unter Eclipse.
- Merging of techniques above and SGNG. Fine Blend system.
- Radial basis function network approximating T_P.
- Very robust with respect to noise and damage.
- Trainable using a version of backpropagation together with techniques from SGNG (Supervised Growing Neural Gas).



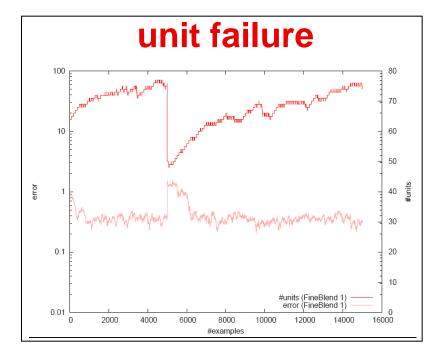
Fine blend vs. SGNG





 $\begin{array}{ccc} \text{target:} & e(0). \\ & e(s(X)) & \leftarrow o(X). \\ & o(X) & \leftarrow \neg e(X) \end{array}$

 $\begin{array}{ll} \text{initial:} & e(s(X)) & \leftarrow \neg o(X) \\ e(X) & \leftarrow e(X) \end{array}$



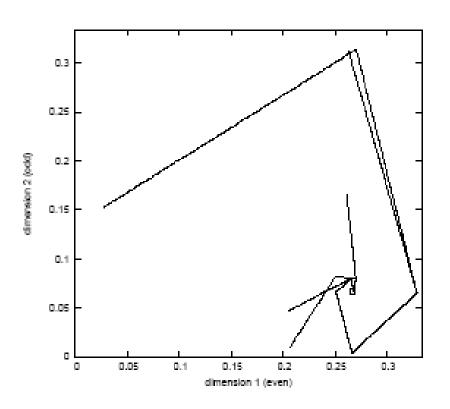


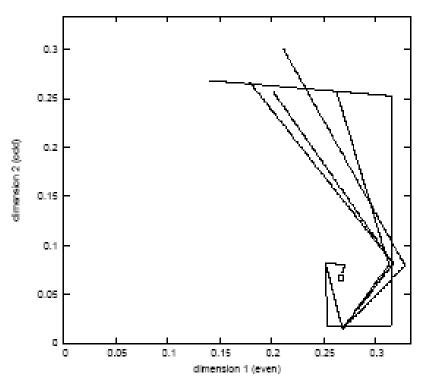
ch Seminar 05/13/2011

Iterating Random Inputs



We observe convergence to unique supported model of the program.





Realised integration



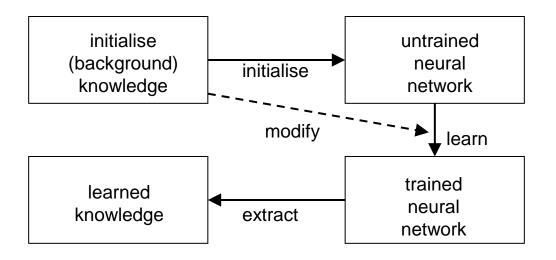
- Neural
 - trainable by backpropagation
 - robust
- Symbolic
 - computes logical model



Realising the cycle: Extraction



- Extraction of PL-knowledge from trained neural networks has never been attempted before.
- Idea: Represent programs and nets in
 \mathbb{N}
 number of weights in net) and search for best approximators using suitable metrics on vectors.



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Outlook



Short term:

- Further experiments and evaluations.
- Develop and realise extraction method.
- Develop concrete application scenarios.
- Realise learning under background knowledge.

Medium and long term:

- Carry over to other KRR paradigms, e.g. DLs.
- Develop integrated connectionist learning and reasoning for cognitive systems applications.

Related work I



- There is hardly any work on first-order neural-symbolic integration.
- M. Lane, A. Seda. Some Aspects of the Integration of Connectionist and Logic-Based Systems. Information, 9(4)(2006), 551-562.
 - Based on the propositional Core Method: Approximation of first-order programs by a finite number of ground instantiated clauses.
 - Purely theoretical.

Related work II



- H. Gust, K.-U. Kühnberger, P. Geibel. Learning Models of Predicate Logical Theories with Neural Networks Based on Topos Theory. In P. Hitzler, B. Hammer (eds.). Perspectives of Neural-Symbolic Integration, Studies in Computational Intelligence 77, Springer, 2007, pp. 233-264.
 - variable-free representation using category theory
 - learns corresponding models
 - running system

Related work III



- Using Bilattice-based annotated logic programs
- Propositional + first-order. Basically a lifting of the Hölldobler & Kalinke approach.
- No running system available
- [Komendantskaya, Seda, 2006]



Related work IV



- Connectionist realisation of proof-theory
- Specifically, SLD-resolution
- Tough ...
- [Komendantskaya, ongoing]



Critical Questions



- The brain doesn't use logic.
 - Well yes. Logic is a (coarse) model. Like Newtonian physics is a coarse model.
 - We DO NEED more neuroscience input!
- The "infinity" discussion doesn't apply to the brain.
 - Well yes. But give me something better.
- So where do you want to apply all this?
 - Good question. We currently have a hammer. We need to find some suitable nails.
 - But we DO HAVE one of the first two approaches to firstorder neural-symbolic integration after 10 years of searching for it!!!!

Collaborators



Thank you for your attention



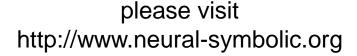






- Artur S. d'Avila Garcez
- Barbara Hammer
- Steffen Hölldobler
- Jens Lehmann
- Kai-Uwe Kühnberger
- Anthony K. Seda
- Andreas Witzel













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- J. Lehmann, S. Bader and P. Hitzler, Extracting reduced logic programs from artificial neural networks, In: Proceedings of the IJCAI-05 Workshop on Neural-Symbolic Learning and Reasoning, NeSy'05, Edinburgh, UK, August 2005.
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