

Neural-Symbolic Integration

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PD Dr. Pascal Hitzler

- Diplom (Mathematics) Univ. of Tübingen 1998
- PhD (Mathematics), Nat. Univ. of Ireland Cork 2001
- 2001-2004 AI Institute TU Dresden
- 2005 Habilitation (Computer Science)
- since 2004 Assistant Professor, AIFB, Univ. of Karlsruhe
 - Knowledge Representation and Reasoning for the Semantic Web
 - Neural-Symbolic Integration
 - Mathematical Foundations of Artificial Intelligence

Main references for this talk

- S. Bader, P. Hitzler, S. Hölldobler. Connectionist Model Generation: A First-Order Approach.
 Neurocomputing. To appear.
- S. Bader, P. Hitzler, S. Hölldobler, A. Witzel. A Fully Connectionist Model Generator for Covered First-Order Logic Programs. In: Manuela M. Veloso, Proceedings of the Twentieth International Joint Conference on Artificial Intelligence, IJCAI-07, Hyderabad, India, January 2007, AAAI Press, Menlo Park CA, 2007, pp. 666-671.
- P. Hitzler, S. Hölldobler and A. K. Seda. Logic Programs and Connectionist Networks. Journal of Applied Logic, 2(3), 2004, 245-272.

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New book:

Barbara Hammer, Pascal Hitzler (eds.)

Perspectives of Neural-Symbolic Integration.

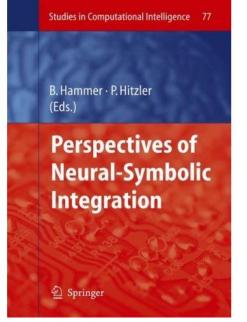
Studies in Computational Intelligence 77. Springer, 2007.

With contributions by

Barreto, de Raedt, Frasconi, Garcez, **Geibel**, **Gust**, Hölldobler, **Kühnberger**, Ritter, Saunders, Seda, Shastri, Sperduti, Tino



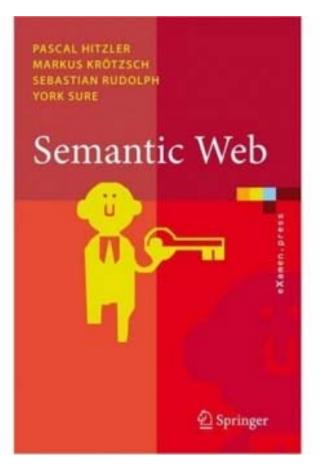
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Another new book

 Hitzler, Krötzsch, Rudolph, Sure Semantic Web – Grundlagen. Springer, 2008. 24,95 €

 First German Textbook on Foundations of the Semantic Web.



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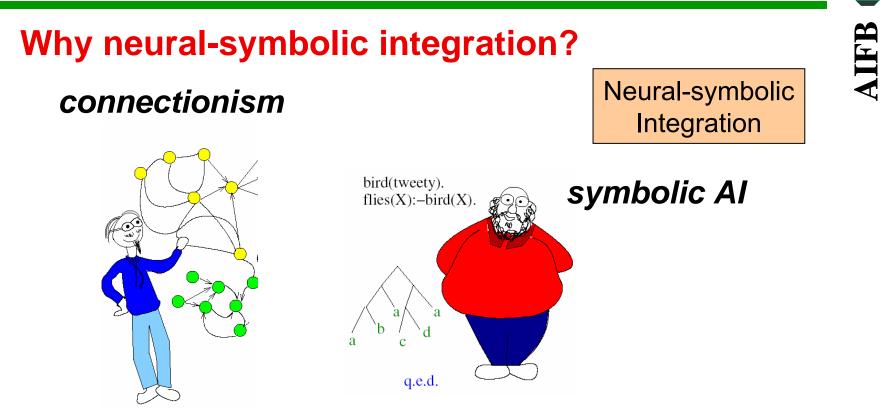
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- 1. Some of my interests
- 2. Why neural-symbolic integration?
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- 6. The cycle for first-order logic
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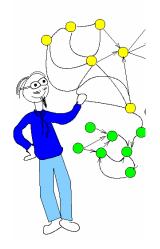
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Neural-symbolic Integration



- Artificial neural networks and symbolic AI are two fundamentally different paradigms in AI.
- Their strengths and weaknesses are complementary.
- *Neural-symbolic Integration* is about integrating the paradigms while retaining their strengths.

Artificial neural networks



- Powerful machine-learning paradigm.
- Inspired by Biology/Neuroscience.
- Learning from noisy data possible.
- Robust. Graceful degradation.
- No declarative semantics. Black boxes.
- Recursive structures difficult.
- Cannot learn with background knowledge.



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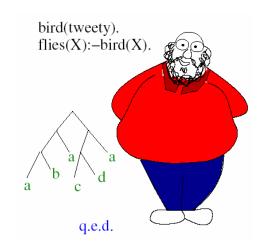
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Knowledge representation/symbolic Al

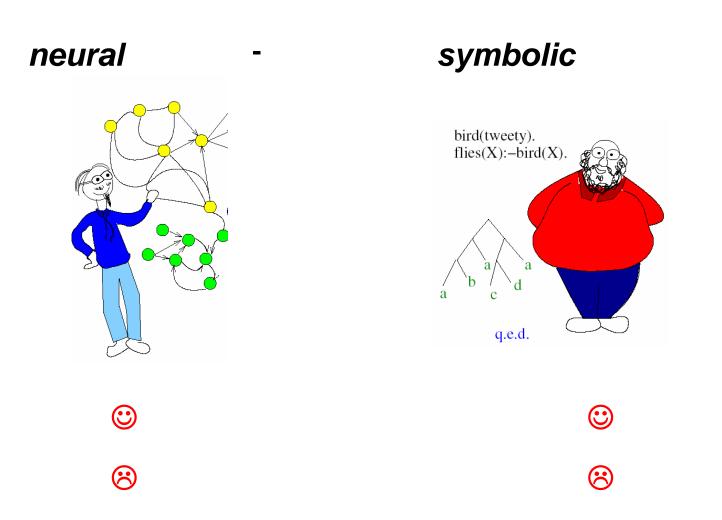
- Logic-based. *Declarative*.
- Modelled from human thinking.
 - Explicit coding of knowledge.
 - Highly recursive.

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- Learning is difficult.
- Hardly tolerant against noise.
- Reasoning has high computational complexity.







realising connectionist processing of symbolic knowledge

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The four main problems of neural-symbolic integration

- Connectionist representation of symbolic knowledge.
- Extraction of symbolic knowledge from artificial neural networks.
- Connectionist learning of symbolic knowledge.
- Learning under background knowledge.

Besides ...



... the *technical* motivation just given:

- neural-symbolic integration is about the study from a computer science perspective – how knowledge can be processed within models of the brain
- standard artificial neural networks appear to be insufficient to capture human knowledge processing
- logic also appears to be insufficient to capture human knowledge processing

Driving motivation

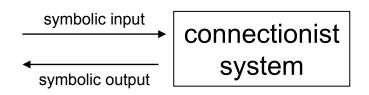
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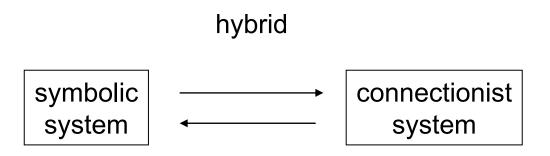
- Our approach is mainly *computer-science-driven*.
 realisation of intelligent systems
- It contributes only indirectly to the question, how humans model reality and think about it.
- At hindsight, our approach probably rather shows, how humans do *not* model reality and think about it.
- Generally, neural-symbolic research requires more input from recent developments in neuroscience!

Hybrid vs. Integrated Approach



integrated





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Earlier work

McCulloch & Pitts 1943

Values 0 ("false") and 1

("true") being

- Neurons with binary activation functions.
- Modelling of propositional connectives.
- Networks equivalent to finite automata.

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1.5

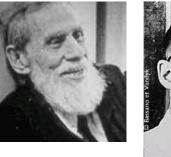
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propagated. Simultaneous update of all nodes in network.



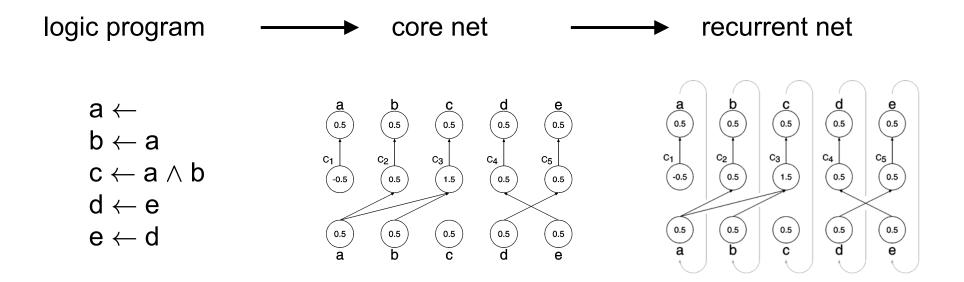


disjunction

conjunction

The propositional Core Method

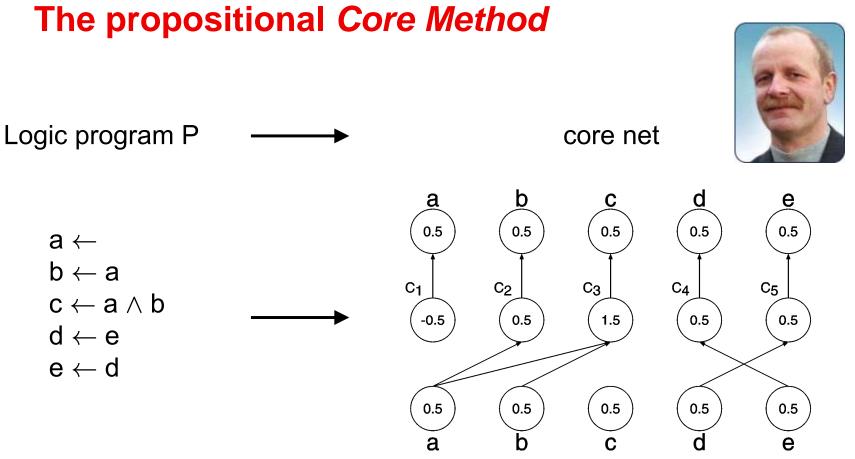
- Hölldobler & Kalinke 1994
 - Extends the approach by McCulloch & Pitts.
 - Representation of propositional logic programs and their semantics.
 - "Massively parallel reasoning."



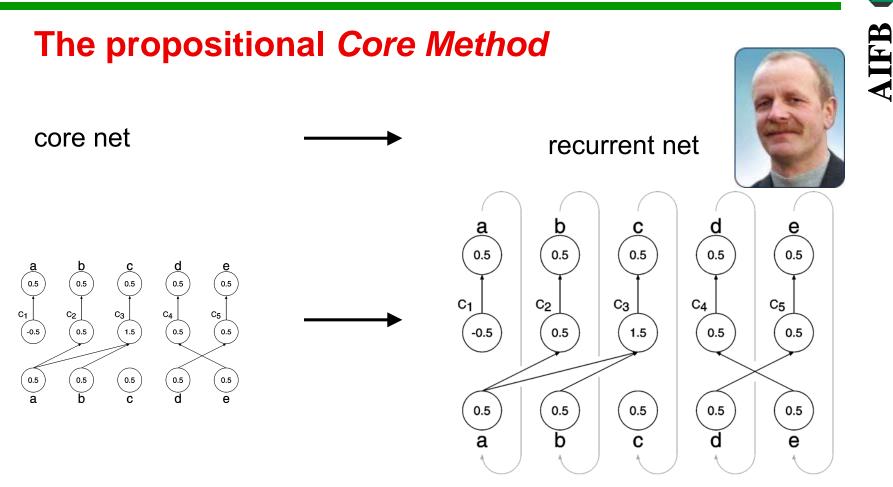








- Update "along implication".
- Corresponds to computing the semantic operator T_P .
- T_P represents meaning (semantics) of P through its fixed points.



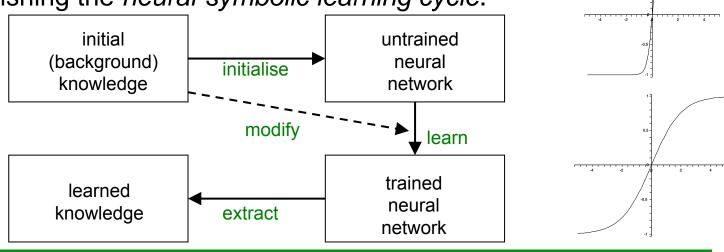
- Repeated updates along layers corresponds to iterations of the semantic operator.
- Semantics of the program (= fixed point of the operator) can be computed in a parallel manner.

CILP – Connectionist Inductive Logic Programming

 Garcez & Zaverucha 1999 Garcez, Broda & Gabbay 2001

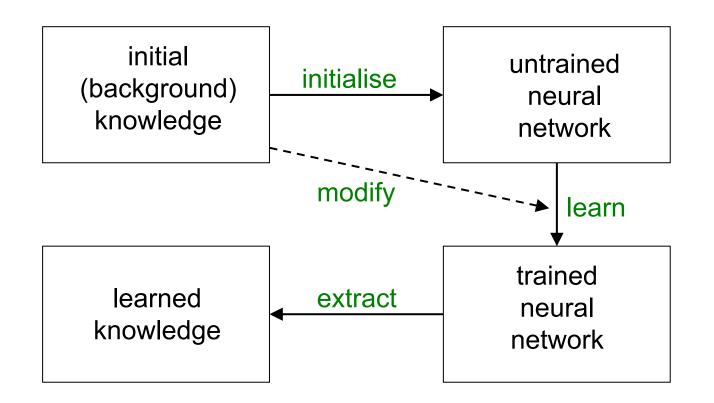


- Development of a learning paradigm from the Core Method.
- Required: differentiable activation function.
 - Allows learning with standard methods.
 - Backpropagation algorithm.
- Establishing the *neural-symbolic learning cycle*.



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The neural-symbolic learning cycle



The four main problems of Neural-symbolic Integration.

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Some new developments on CILP

- We carried over the approach to *Description Logic Programs* (DLP).
- Although not propositional, DLP lends itself to a propositional handling.
- Its special nature allows for some *data compression*, which enables to use CILP on large knowledge bases.
- Result: First neural-symbolic learning paradigm for an ontology language!

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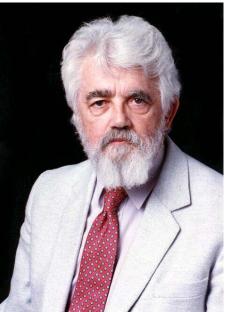
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 Connectionist representation of PL-knowledge very hard to realise.
 McCarthy 1988: "Propositional fixation."

We need to capture the infinite in a finite way.

- infinite ground instantiations
 (∀x) male(x) ∧ hasSon(x,son(x)) → father(x)
- term representations member(X, [a,b,c | [d,e]])
- variable bindings male(x) \land hasSon(x,y) \rightarrow father(x)



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PL Core Method

 Hölldobler, Kalinke, Störr 1999 Hitzler, Hölldobler, Seda 2004



- Idea:
 - Use results by Funahashi 1989: "Every continuous function on the reals is approximable by standard feedforward networks. "
 - Hence: Consider logic programs for which T_P-operator is continuous in this sense.

Funahashi 1989 (simplified)

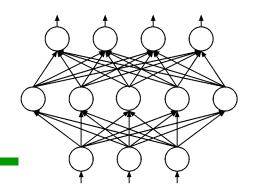
- σ sigmoidal activation function
- $K \subseteq \mathbb{R}$ compact
- f: $K \to R$ continuous
- c > 0

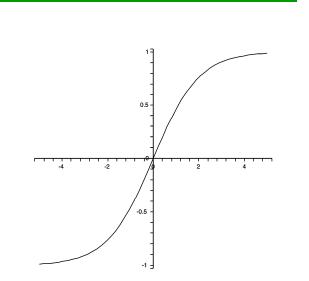
Then there exists a three-layer feedforward network with activation function σ and I/O-function F, so that

$$\max_{x \in \mathsf{K}} \{ d(\mathsf{f}(x), \mathsf{F}(x)) \} < \varepsilon.$$

Here d is a metric which induces the natural topology on R.

I.e. continuous functions can be *uniformly approximated* by such networks with arbitrary accuracy.







Continuity of $T_P - I$



- Hitzler, Hölldobler, Seda 2004
- Let \mathcal{B}_A be the set of all body atoms in ground instantiated clauses of P with head A.

 $\begin{array}{l} \mathsf{T}_{\mathsf{P}} \colon \mathsf{I}_{\mathsf{P}} \to \mathsf{I}_{\mathsf{P}} \text{ is called locally finite, if} \\ \text{ for all atoms A and all } \mathsf{I} \in \mathsf{I}_{\mathsf{P}} \\ \text{ there exists a finite } \mathsf{S} \subseteq \mathcal{B}_{\mathsf{A}}, \\ \text{ such that } \mathsf{T}_{\mathsf{P}}(\mathsf{J})(\mathsf{A}) = \mathsf{T}_{\mathsf{P}}(\mathsf{I})(\mathsf{A}) \\ \text{ for all } \mathsf{J} \in \mathsf{I}_{\mathsf{P}} \text{ which coincide with I on S.} \end{array}$

$$p(s(x)) \leftarrow p(x).$$

 $p(0)$
 $p(x) \leftarrow p(s(x)).$

e.g. $\mathcal{B}_{p(s(0))} = \{p(0), p(s(s(0)))\}$

Continuity of $T_P - II$



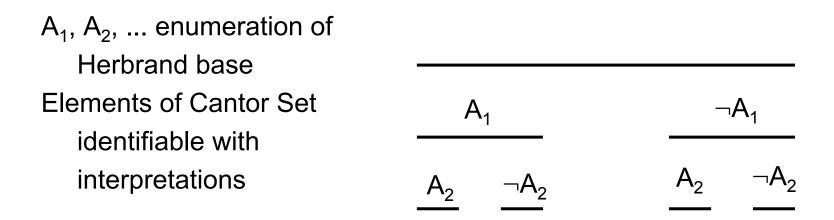
 $T_P: I_P \rightarrow I_P$ is locally finite iff T_P is continuous in Cantor space.

- Cantor-continuity is continuity wrt. the Cantor topology on the Cantor set.
- The Cantor topology is homeomorphic to the prefix-distance on (infinite) binary trees.
- The Cantor topology is homeomorphic to the subspace topology which is induced on a subset of R which is compact, totally disconnected and dense in itself.

Continuity of T_P – III



- There are (uncontably) many homeomorphisms which map I_P with the Cantor topology into suitable subsets of R.
- Locally finiteness is a logical (topology-free) characterisation of logic programs which can be represented in a a connectionist way in the sense of Funahashi.
- Problem: this argumentation is not constructive!



IFB **Relationship of I_P to Cantor Space** Interpretations with T_{P} Cantor topology (I_P,Q) (I_P,Q) Homeomorphism l $\iota(\mathsf{T}_\mathsf{P})$ Cantor Cantor Cantor space as compact subspace of R Georg Cantor



The Cantor topology as a paradigm bridge

- Connectionist side:
 - Cantor topology is a subtopology of the usual topology on the real numbers
- Logic Programming side:
 - Cantor topology captures useful notions of convergence of semantic operators, e.g. If $T_P^n \rightarrow I$ (for $n \rightarrow \infty$), then I is a model of P.



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Realising the cycle: Representation of symbolic knowledge

- Bader, Hitzler, Hölldobler, Witzel IJCAI-07
 - Algorithm for the approximate construction of neural networks from logic programs.
 - Realised for
 - RBS nets with triangular activation function
 - RBF nets with raised cosine activation function

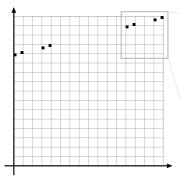
$$\tau_{w,h,m}(x) = \begin{cases} \frac{h}{2} \cdot \left(1 + \cos\left(\frac{\pi(x-m)}{w}\right)\right) & \text{if } |x-m| < w \\ 0 & \text{otherwise} \end{cases}$$

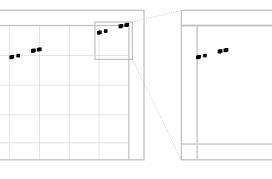
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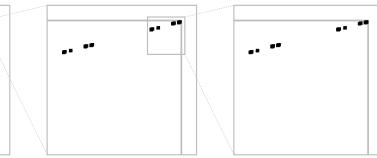


Realising the cycle (first-order representation)

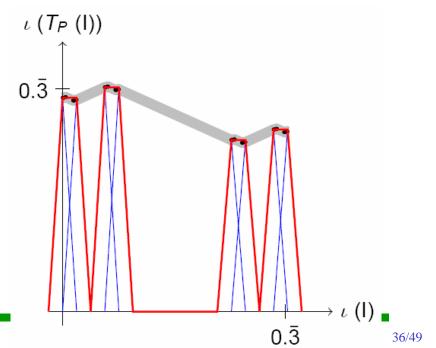




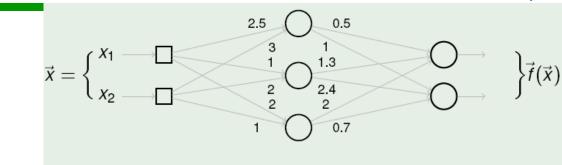




- Graph of T_P is a fractal.
- Approximation up to arbitrary precision possible.
- Requires quite some calculation to get correct parameters in higher dimensions ...



Hitzler Neural-Symbolic Integration Osnabrück Germany November 2007



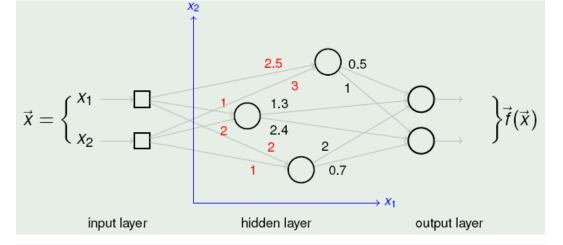
hidden layer

Alf B

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Local representation

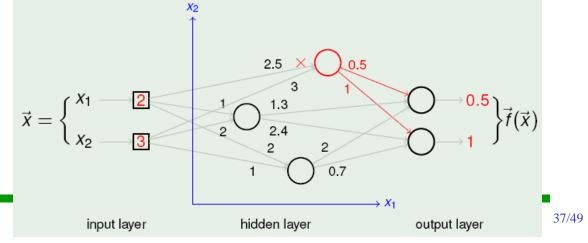
input layer



output layer

and

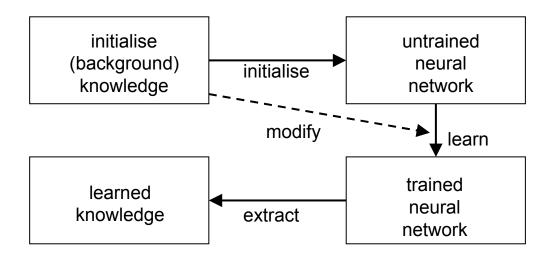
domination of output by one unit



Realising the cycle: learning



- Reuse of standard network architecture allows to use known and powerful learning methods.
 - Backpropagation
 - We merged in techniques from Supervised Growing Neural Gas (SGNG) [Fritzke 1998].



Realising the cycle: Implementation

- Bader & Witzel, first prototype
- JDK 1.5 unter Eclipse.
- Merging of techniques above and SGNG. *Fine Blend* system.
- Radial basis function network approximating T_P.
- Very robust with respect to noise and damage.
- Trainable using a version of backpropagation together with techniques from SGNG (Supervised Growing Neural Gas).

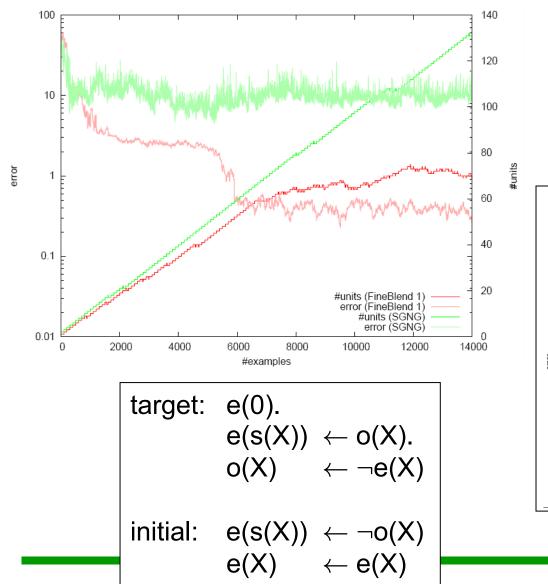




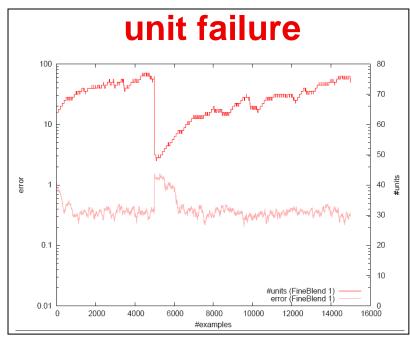


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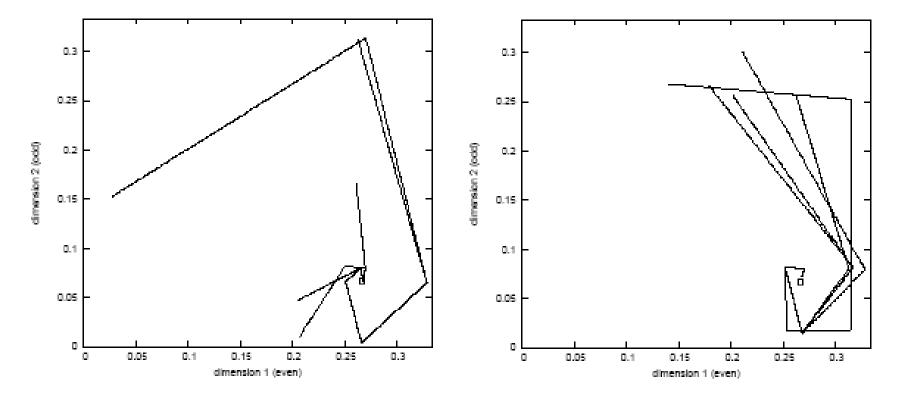




Iterating Random Inputs

We observe convergence to unique supported model of the program.





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Realised integration

- Neural
 - trainable by backpropagation
 - robust
- Symbolic
 - computes logical model

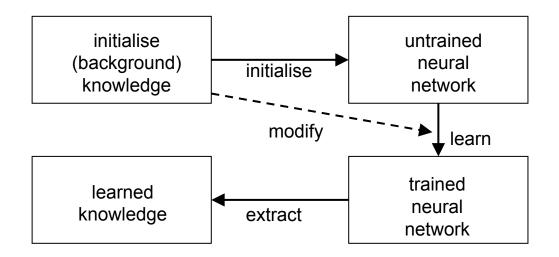






Realising the cycle: Extraction of symbolic knowledge

- Extraction of PL-knowledge from trained neural networks has never been attempted before.
- Idea: Represent programs and nets in Rⁿ (with n = number of weights in net) and search for best approximators using suitable metrics on vectors.



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Outlook

Short term:

- Further experiments and evaluations.
- Develop and realise extraction method.
- Develop concrete application scenarios.
- Realise learning under background knowledge.

Medium and long term:

- Carry over to other KRR paradigms, e.g. DLs.
- Develop integrated connectionist learning and reasoning for cognitive systems applications.

Related work I

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- There is hardly any work on first-order neuralsymbolic integration.
- M. Lane, A. Seda. Some Aspects of the Integration of Connectionist and Logic-Based Systems. Information, 9(4)(2006), 551-562.
 - Based on the propositional Core Method: Approximation of first-order programs by a finite number of ground instantiated clauses.
 - Purely theoretical.

Related work II

- H. Gust, K.-U. Kühnberger, P. Geibel. Learning Models of Predicate Logical Theories with Neural Networks Based on Topos Theory. In P. Hitzler, B. Hammer (eds.). Perspectives of Neural-Symbolic Integration, Studies in Computational Intelligence 77, Springer, 2007, pp. 233-264.
 - variable-free representation using category theory
 - learns corresponding models
 - the authors are among the audience!

Critical Questions

- The brain doesn't use logic.
 - Well yes. Logic is a (coarse) model. Like Newtonian physics is a coarse model.
 - We DO NEED more neuroscience input!
- The "infinity" discussion doesn't apply to the brain.
 - Well yes. But give me something better.
- So where do you want to apply all this?
 - Good question. We currently have a hammer. We need to find some suitable nails.
 - But we DO HAVE one of the first two approaches to first-order neural-symbolic integration after 10 years of searching for it!!!!

Thank you for your attention



Collaborators

- Sebastian Bader
- Artur S. d'Avila Garcez
- Steffen Hölldobler
- Jens Lehmann
- Sebastian Rudolph
- Anthony K. Seda
- Andreas Witzel

please visit http://www.neural-symbolic.org







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- S. Bader, P. Hitzler and A. Witzel, Integrating First Order Logic Programs and Connectionist Systems - A Constructive Approach, In: Proceedings of the IJCAI-05 Workshop on Neural-Symbolic Learning and Reasoning, NeSy'05, Edinburgh, UK, August 2005.

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- Sebastian Rudolph, Encoding Closure Operators into Neural Networks. Poceedings of the IJCAI-07 Workshop on Neural-Symbolic Learning and Reasoning, NeSy'07, Hyderabad, India, January 2007.

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